

	EXPRESSION	MATHEMATICA SYNTAX
DERIVATIVES AND GRADIENTS	Partial derivatives of $f : \mathbb{R}^n \rightarrow \mathbb{R}$ $f_x = \frac{\partial f}{\partial x}$ $f_y = \frac{\partial f}{\partial y}$	D[f[x,y], x] or D[f[x,y,z], x], etc. D[f[x,y], y] or D[f[x,y,z], y], etc.
	Partial derivatives of $f : \mathbb{R}^n \rightarrow \mathbb{R}^m$ $\frac{\partial f_1}{\partial x}$ $\frac{\partial f_2}{\partial x}$	D[f[x,y][[1]], x] or D[f[x,y,z][[1]], x], etc. D[f[x,y][[2]], x] or D[f[x,y,z][[2]], x], etc. (alternatively, compute total derivative using the command given below, and read off the answer)
	Higher-order partial derivatives of $f : \mathbb{R}^n \rightarrow \mathbb{R}$ $f_{xx} = \frac{\partial^2 f}{\partial x^2}$ $f_{yyyy} = \frac{\partial^5 f}{\partial y^5}$ $f_{xy} = \frac{\partial^2 f}{\partial x \partial y}$ $\frac{\partial^{10} f}{\partial x^3 \partial y^2 \partial z^5}$	D[f[x,y], x,x] or D[f[x,y], {x,2}] D[f[x,y,z], {y,5}] D[f[x,y], x,y] D[f[x,y,z], {x,3},{y,2},{z,5}]
	Total derivative of $f : \mathbb{R}^n \rightarrow \mathbb{R}^m$	D[f[x,y], {x,y}] or D[f[x,y,z], {x,y,z}], etc. (to get the answer as matrix, click MatrixForm)
	Total derivative of $f : \mathbb{R} \rightarrow \mathbb{R}^m$	f'[x] or f'[t], etc. (f''[x] and f''[x] do the obvious things)
	Gradient ∇f	Grad[f[x,y], {x,y}] or Grad[f[x,y,z], {x,y,z}], etc. (or use total derivative command given above)
Directional derivative $D_u f(\mathbf{x})$	Grad[f[x,y], {x,y}].Normalize[u] or Grad[f[x,y,z], {x,y,z}].Normalize[u]	

To substitute numerical values for x, y and z , do one of two things:

1. Define the derivative as a function of x, y and z , then ask *Mathematica* to plug in the values of x, y and z to your newly-defined function:

Example: Suppose you wanted to compute $f_{xy}(3, 2, -5)$. You could execute these commands, one at a time:

```
h[x_,y_,z_] = D[f[x,y,z], x, y]
h[3,2,-5]
```

2. Follow any of the commands above with some syntax that causes *Mathematica* to substitute in numbers for the variables:

Example: Suppose you wanted to compute $f_{xy}(3, 2, -5)$. You could execute this single command:

```
D[f[x,y,z], x, y] /.x->3 /.y->2 /.z->-5
```

In general, you follow the command with a series of `/.var->number` commands; this plugs in *number* to variable *var* in the preceding expression.